# **2024 Fall Midterm**



### **Exam Type:** A

A "closed book" examination. No aids are permitted other than the information printed on the examination paper.

### **Calculator Type:** 3

Non-programmable calculators from a list of approved calculators as issued by the Faculty Registrar.

#### **Instructions:**

**Do not** write answers on the back of pages as they will not be graded. Use the blank sheet at the end of the exam for extra space, and clearly indicate in the provided answer space if your response continues.

If a question seems unclear or ambiguous, state your assumptions and answer accordingly. In case of an error, identify it, provide a corrected version, and respond as if the question has been fixed.

Provide brief and specific answers. Clear and concise responses will receive higher marks compared to vague and wordy ones. Note that marks will be deducted for incorrect statements in your answers.

Below is a partial listing of GCC's optimize options.

-O1 turns on the following optimization flags:

```
-fcompare-elim
-fcprop-registers
-fdce
-fdefer-pop
-fdelayed-branch
-fdse
-fguess-branch-probability
-fif-conversion
-fif-conversion2
-finline-functions-called-once
-fipa-modref
-fipa-reference
-fipa-reference-addressable
-fmerge-constants
-fmove-loop-invariants
-fmove-loop-stores
-ftree-bit-ccp
-ftree-ccp
-ftree-ch
-ftree-coalesce-vars
-ftree-copy-prop
-ftree-dce
-ftree-dse
-funit-at-a-time
```
-O2 turns on all previous optimization flags, and additionally:

```
-fcode-hoisting
-fcse-follow-jumps -fcse-skip-blocks
-ffinite-loops
-fgcse -fgcse-lm
-finline-functions
-finline-small-functions
-fipa-bit-cp -fipa-cp -fipa-icf
-fipa-ra -fipa-sra -fipa-vrp
-flra-remat
-foptimize-strlen
-fpartial-inlining
-fpeephole2
-fstore-merging
-fstrict-aliasing
-fthread-jumps
-ftree-builtin-call-dce
-ftree-loop-vectorize
-ftree-pre
-ftree-slp-vectorize
```

```
-ftree-tail-merge
```
### **Short Answer (15 marks total)**

**Q1 (1 mark). True / False** (Circle the correct answer)

Latency(L1 cache) < Latency(register) < Latency(Main Memory).

**Q2 (1 mark). True)/ False** (Circle the correct answer)

Latency(Main Memory) is 2 order of magnitude larger than Latency(L1 cache).

**Q3 (1 mark). True / (False**) (Circle the correct answer)

Last Level Cache ususally refers to level 2 cache in a server CPU.

**Q4 (1 mark).** (True) False (Circle the correct answer)

If you can only speed up 50% of your code, the best overall speedup you can achieve is 2x.

## **Q5 (1 mark). True / False** (Circle the correct answer)

A program running on a processor with a lower Cycle-Per-Instruction (CPI) always runs faster than on a processor with higher CPI.

## **Q6 (1 mark). True / False** (Circle the correct answer)

With Out-Of-Order superscalar processors, the Instruction-Per-Cycle (IPC) of a program can always be larger than 1.

**Q7 (1 mark).** True / (False) (Circle the correct answer)

Compiler optimizations can effectively reduce compulsary cache misses.

**Q8 (1 mark). True / (False)** (Circle the correct answer)

Programmers can adjust cache associativity to reduce conflict cache misses.

**Q9 (1 mark). True / False** (Circle the correct answer) A 4-way set associative cache has a 4 sets per line.

**Q10 (1 mark). True / False** (Circle the correct answer)

gcc compiler with -O2 option typically invokes inter-procedural link-time optimizations.

**Q11 (1 mark).** (True) False (Circle the correct answer)

Performance profilers typically use instrumentation-based method, or sampling-based method, or both.

**Q12 (1 mark). True / (False**) (Circle the correct answer)

A program with frequent TLB misses but not page faults has a working set larger than main memory.

**Q13 (1 mark).** (True) False (Circle the correct answer)

A physical address can correspond to multiple different virtual addresses in different processes.

## **Q14 (1 mark). True / False** (Circle the correct answer)

Memory references are dictated by an application's algorithmic behavior and therefore a programmer can do little to enhance the application's temporal or local locality.

## **Q15 (1 mark). True / False** (Circle the correct answer)

Consider an SRAM-based cache for a DRAM-based main memory. Neglect the possibility of other caches or levels of the memory hierarchy below main memory. If a cache is improved, increasing the typical hit rate from 98% to 99%, the typical average memory access time will be improved by 1%.

#### **Compiler Optimization (8 marks total)**

```
#define A (9)
#define B (2)
static int foo(int x, int y) {
 if (x + A > y * B) {
   return x;
 } else {
   return y;
 }
}
int main(void) {
 int x, y, z;
 x = 4;y = 7;z = foo(y, x);return z;
}
```
**Q16 (8 marks).** List 3 types of optimizations that the compiler can perform on the code shown above. Briefly describe how these optimizations would be applied. Also, show the final optimized main function.

```
1. Constant Propagation & Folding
 2. Copy Propagation
 3. Inlining
 4. Dead Code Elimination
int main(void) {
  return 7;
```

```
}
```
#### **Program Optimization (6 marks total)**

Consider the following code that computes the minimum of the pairwise sum of two vectors:

```
#include <limits.h>
#define MIN(x,y) ((x) < (y) ? (x) : (y))
#define INFINITY INT64_MAX
typedef struct { int64_t* data; int len; } vec_t;
int vec_length(<math>vec_t * v</math>) { return <math>v</math>-<math>len</math>; }int64_t vec_elem( vec_t*v, int i ) { return v->data[i]; }
void vec_init( vec_t* v, int len ) { v->len = len; v->data = calloc( sizeof(int64_t)*len ); }
void vec_fini( vec_t* v ) { free(v->data); }
void minsum( vec_t* a, vec_t* b, int64_t* result)
{
        *result = INFINITY;
        for (int i = 0; i < vec\_len(a); i++)*result = MIN(*result, vec_elem(a,i)+vec_elem(b,i));
}
```
**Q17 (6 marks).** Use the techniques learned in class to improve the implementation above. Clearly name the techniques utilized (You do not need to do loop unrolling). Show your final optimized minsum function.

Name 2 of:

```
1. Inlining
 2. Loop-Invariant Code Motion
 3. Local Variable (Reduction Recognition)
void minsum(vec_t* a, vec_t* b, int64_t* result)
{
   int64_t temp = INFINITY;
   int len = a->len;
   for (int i = 0; i < 1en; i^{++}) {
       temp = MINtemp, a->data[i], b->data[i]);}
   *result = temp;
}
```
### **Cache Hierarchy (11 marks total)**

The memory hierarchy of a 32-bit machine has 4 GB byte-addressable main memory and one-level data cache with no prefetching. The data cache is two-way set-associative, has a block size of 32 bytes and can store 2KB of data. The cache uses LRU as its replacement policy. Assume that the cache lines are initially invalid.

**Q18 (3 marks).** Calculate the number of bits needed for the cache tag, index, and offset.

```
tag: 22 bits, index: 5 bits, offset: 5 bits
```
Consider the following code, which calls the minsum function developed on the previous page.

```
vec_t a, b;
int main(void) {
  int64_t result;
  vec_init(&a, 256);
  vec_init(&b, 256);
  minsum(&a, &b, &result);
  return result;
}
```
You can assume the following:

1. sizeof $(int64_t) = 8$ 

2. Array begins at memory location 0x0

3. The only memory accesses are to the array entries. All other variables are stored in registers.

**Q19 (4 marks).** What is the cache miss rate when this code is run? Recall that miss rate is defined as #misses / #accesses.

25%

Consider the following code.

vec\_t a;

```
int main(void) {
  int64_t result;
  vec_init(&a, 256);
  minsum(&a, &a, &result);
  return result;
}
```
**Q20 (2 marks).** What is the cache miss rate when this code is run?

12.5%

**Q21 (2 marks).** What would be the cache miss rate if the code shown in **Q19** is run on a machine with a direct-mapped cache, with the same block size (32 bytes) and storage (2KB of data)?

100%

### **Virtual Memory (12 marks total)**

**Q22 (1 mark).** Which of these features in a system best justify the use of at two-level page table structure, as opposed to a one level page table structure? (Circle the correct answer)

(a) Small page sizes **[Correct]**

(b) Frequent memory accesses

(c) High degree of spatial locality in programs

(d) Sparse memory usage patterns

**Q23 (1 mark).** Which section of an ELF file contains the compiled functions from a program?

(Circle the correct answer)

(a) .data

(b) .rodata

(c) .text **[Correct]**

(d) .bss

**Q24 (10 marks).** Assume a system that has:

- 1. A two way set associative TLB
- 2. A TLB with 8 total entries
- 3. 2 <sup>8</sup> byte page size
- 4. 2 <sup>16</sup> bytes of virtual memory

Assume TLB has the following content (Recall that a TLB is like a cache: with index equivalent to set number, frame number equivalent to cache block content):



Fill in the table below. Strike out anything that you don't have enough information to fill in.



### **Dynamic Memory (8 marks total)**

Consider the follow code fragment:

**struct** { **char** \*a; **short** b; **double** c; **char** d; **float** e; **char** f; **int** g; **void** \*h; } foo;

**Q25 (1 mark).** Show how the struct above would appear on a 32-bit Linux machine (primitives of size k are k-byte aligned). Label the bytes that belong to the various fields with their names and clearly mark the end of the struct. Cross out any bytes that are allocated in the struct but are not used.



**Q26 (1 mark).** Rearrange the above fields in foo to conserve the most space in the memory below. Label the bytes that belong to the various fields with their names and clearly mark the end of the struct. Cross out any bytes that are allocated in the struct but are not used.

d	$\mathsf f$	$\mathsf b$	b	a	a	a	a
Byte 0	Byte 1	Byte 2	Byte 3	Byte 4	Byte 5	Byte 6	Byte 7
$\mathbf C$	$\mathbf C$	${\bf c}$	$\mathbf C$	$\mathbf c$	$\mathbf C$	$\mathbf C$	$\mathbf c$
Byte 8	Byte 9	Byte 10	Byte 11	Byte 12	Byte 13	Byte 14	Byte 15
e	e	$\mathbf e$	e	g	$\mathbf g$	$\mathsf g$	g
Byte 16	Byte 17	Byte 18	Byte 19	Byte 20	Byte 21	Byte 22	Byte 23
h	h	h	h				
Byte 24	Byte 25	Byte 26		Byte 27 $e_1$ d Byte 28	Byte 29	Byte 30	Byte 31
Byte 32	Byte 33	Byte 34	Byte 35	Byte 36	Byte 37	Byte 38	Byte 39

**Q27 (6 marks).** Compare the three classic memory management algorithms on their asymptotic complexity in the following Table, assuming the peak number of memory blocks (including allocated blocks and free blocks) is M, the peak number of free memory blocks is N. Use the Big O notation for asymptotic complexity.

