

Lecture 06 - Dependencies

ECE 459: Programming for Performance

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Previously

- We saw race conditions and how to remedy them with **synchronization**
- I forgot to mention barriers too, useful if you want threads to wait at a certain point in execution for x other threads to finish
- `pthread_barrier_t`, with `init` (takes as a parameter how many threads it should wait for) and `destroy`
- Also has `wait` which is similar to a `join` that will wait for the specified number of threads to arrive at the barrier

Today

- I talked before about **dependencies** being the main limitation to parallelization
- Basically, when a computation has to be evaluated as XY instead of YX
- We are just going to assume there is no synchronization problems for these examples (although they exist too)
- Only trying to identify code that is safe to run in parallel

Memory-carried Dependencies

- Dependencies limit the amount of parallelization in a program

Can we execute these 2 lines in parallel?

```
x = 42  
x = x + 1
```

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No

- What are the possible outcomes? (x is initially 1)

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```
x = 42  
x = x + 1
```

No

- What are the possible outcomes? (x is initially 1)
 $x = 43$ or $x = 42$

Read After Read (RAR)

Can we execute these 2 lines in parallel? (initially x is 2)

```
y = x + 1  
z = x + 5
```

Read After Read (RAR)

Can we execute these 2 lines in parallel? (initially x is 2)

```
y = x + 1  
z = x + 5
```

Yes

- The variables y and z are independent
- Variable x is only read

Read After Write (RAW)

What about these 2 lines? (again, initially x is 2)

```
x = 37  
z = x + 5
```

Read After Write (RAW)

What about these 2 lines? (again, initially x is 2)

```
x = 37  
z = x + 5
```

No, $z = 42$ or $z = 7$

- We cannot change the order
- Also known as a **true dependency**

Write After Read (WAR)

What if we change the order? (again, initially x is 2)

```
z = x + 5  
x = 37
```

Write After Read (WAR)

What if we change the order? (again, initially x is 2)

```
z = x + 5  
x = 37
```

No, again, $z = 42$ or $z = 7$

- Also known as a **anti-dependency**
- We can modify the code to run these lines in parallel

Removing Write After Read (WAR) Dependency

Make a copy of the variable

```
x_copy = x  
z = x_copy + 5  
x = 37
```

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```
x_copy = x
z = x_copy + 5
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```

We can run the 2 lines in parallel now

- There is now true dependency (RAW) between the 2 lines
- Why is this useful?

Removing Write After Read (WAR) Dependency

Make a copy of the variable

```
x_copy = x
z = x_copy + 5
x = 37
```

We can run the 2 lines in parallel now

- There is now true dependency (RAW) between the 2 lines
- Why is this useful?

```
z = very_long_function(x) + 5
x = very_long_calculation()
```

Write After Write (WAW)

Can we run these lines in parallel? (initially x is 2)

```
z = x + 5  
z = x + 40
```


Write After Write (WAW)

Can we run these lines in parallel? (initially x is 2)

```
z = x + 5  
z = x + 40
```

Nope, $z = 42$ or $z = 7$

- Also known as a **output dependency**
- We may remove this dependency (similar to WAR)

Write After Write (WAW)

Can we run these lines in parallel? (initially x is 2)

```
z = x + 5  
z = x + 40
```

Nope, $z = 42$ or $z = 7$

- Also known as a **output dependency**
- We may remove this dependency (similar to WAR)

```
z_copy = x + 5  
z = x + 40
```

Summary of Memory-carried Dependencies

		Second Access	
		Read	Write
First Access	Read	No Dependency Read After Read (RAR)	Anti-dependency Write After Read (WAR)
	Write	True Dependency Read After Write (RAW)	Output Dependency Write After Write (WAW)

Loop-carried Dependencies (1)

Can we run these lines in parallel? (initially $a[0]$ and $a[1]$ are 1)

```
a[4] = a[0] + 1  
a[5] = a[1] + 2
```

Loop-carried Dependencies (1)

Can we run these lines in parallel? (initially $a[0]$ and $a[1]$ are 1)

```
a[4] = a[0] + 1  
a[5] = a[1] + 2
```

Yes

- There are no dependencies between these lines
- However, this is not how we normally use arrays...

Loop-carried Dependencies (2)

What about this? (all elements are initially 1)

```
for (int i = 1; i < 12; ++i)
    a[i] = a[i-1] + 1
```

Loop-carried Dependencies (2)

What about this? (all elements are initially 1)

```
for (int i = 1; i < 12; ++i)
    a[i] = a[i-1] + 1
```

No, $a[2] = 3$ or $a[2] = 2$

- Statements are dependent on the previous iteration of the loop
- This is an example of a **loop-carried dependency**

Loop-carried Dependencies (3)

Can we parallelize this loop? (again, all elements are initially 1)

```
for (int i = 4; i < 12; ++i)
    a[i] = a[i-4] + 1
```


Loop-carried Dependencies (3)

Can we parallelize this loop? (again, all elements are initially 1)

```
for (int i = 4; i < 12; ++i)
    a[i] = a[i-4] + 1
```

Yes, to a degree

- We can execute 4 statements in parallel
 - $a[4] = a[0] + 1$, $a[8] = a[4] + 1$
 - $a[5] = a[1] + 1$, $a[9] = a[5] + 1$
 - $a[6] = a[2] + 1$, $a[10] = a[6] + 1$
 - $a[7] = a[3] + 1$, $a[11] = a[7] + 1$

Loop-carried Dependencies (3)

Can we parallelize this loop? (again, all elements are initially 1)

```
for (int i = 4; i < 12; ++i)
    a[i] = a[i-4] + 1
```

Yes, to a degree

- We can execute 4 statements in parallel
 - $a[4] = a[0] + 1$, $a[8] = a[4] + 1$
 - $a[5] = a[1] + 1$, $a[9] = a[5] + 1$
 - $a[6] = a[2] + 1$, $a[10] = a[6] + 1$
 - $a[7] = a[3] + 1$, $a[11] = a[7] + 1$

Always consider the dependencies between iterations

Summary

- Identify memory-carried dependencies
 - 3 types of dependencies (RAW, WAR, WAW)
- How to remove output and anti-dependencies
- Identify loop-carried dependencies
 - Explain dependencies between iterations